

# Estimation Of The Fundamental Frequency Of The Speech signal Compressed By G.729 Algorithm Using PCC Interpolation

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**Abstract**—This paper gives the estimation of the fundamental frequency ( $F_0$ ) of the speech signal modeled by the G.729 method. The estimation of the  $F_0$  was performed by the Peaking-Peaks algorithm with the implemented Parametric Cubic Convolution (PCC) interpolation. The efficiency of PCC was tested for Keys, Greville and Greville two-parametric kernel. The window that gives optimal results was chosen according to the MSE results. At the end, the comparative analysis of the  $F_0$  estimation compressed by G.729 and G.723.1 codec is made.

**Keywords**- Speech processing; Speech compression; Fundamental frequency; VoIP;

## I. INTRODUCTION

ITU-T Telecommunication standardization sector of ITU (International Telecommunication Union) has defined the standard H.324 for specification of components, protocols and procedures which make multimedial communication services in networks with packets communication possible [1]. Besides, H.324 defines audio and video codecs (coders-decoders). G.729 and G.723.1 are audio codecs intensively used in VoIP (Voice over IP) communications [2,3]. G.723.1 provides the speech compression to 5.3 kb/s and 6.3 kb/s. In the first case ACELP (Algebraic Code Excited Linear Prediction) algorithm and in the second MP-MLQ (Multipulse MAXimum Likelihood Quantization) algorithm are applied [3,4]. The frame size is 30 ms with 240 samples with sampling of 8 kHz. Each frame is being processed in the following 7.5 ms. The frame is divided into smaller frames whose duration is 7.5 ms. Delaying (67-97 ms), delaying variations, packets losses and echo influence on the quality of speech transmitted by means of packet network. Evaluation of MOS (Mean Opinion Score) test is acceptable 3.4 (5.3 kbps) and good 3.8 (6.3 kbps) [5]. Recommendation ITU-T Rec. G.729 contains the description of an algorithm for the coding of speech signals at 8 kbit/s using Conjugate-Structure Algebraic-Code-Excited Linear-Prediction (CS-ACELP) [2]. The CS-ACELP coder is based on the Code-Excited Linear-Prediction (CELP) coding model. The coder operates on speech frames of 10 ms corresponding to 80 samples at a sampling rate of 8 kHz. For every 10 ms frame, the speech signal is analyzed to extract the parameters of the CELP model (linear-prediction filter coefficients, adaptive and fixed-codebook indices and gains). These parameters are encoded and transmitted [6]. At the decoder, these parameters are used to retrieve the excitation and synthesis filter parameters. The speech is reconstructed by filtering this excitation through the short-term synthesis filter. The short-term synthesis filter is based on a 10th order Linear Prediction (LP) filter. The long-term, or pitch synthesis filter is implemented using the so-called adaptive-codebook approach. After computing the reconstructed speech, it is further enhanced by a postfilter. This coder encodes speech and other audio signals with 10 ms frames. In addition, there is a look-ahead of 5 ms, resulting in a total algorithmic delay of 15 ms. Evaluation of MOS test is good 3.84 (6.3 kbps) [7]. With G.723.1 and G.729 coding the  $F_0$  estimation is firstly being done, and then the estimated  $F_0$  is used in the following steps of the speech signal coding. In the decoding process the speech signal is reconstructed which implies renewal of the  $F_0$  [8,9].

After the transfer of the speech signal by the VoIP service, on the reception side there is a need for the signal processing (speech and speaker recognition, echo canceling, improvement of the quality and the speech articulateness etc.). The characteristic example is the correction of the speech signal quality by reducing of dissonant frequencies [10,11]. In the speech signal processing there is a need for determination of the  $F_0$ . A number of algorithms were developed for determination of the  $F_0$  where the analysis is performed in the time and frequency domain [12-15].

The frequently applied method for determination of the  $F_0$  is based on the peaking peaks of the amplitude characteristic in the specific frequency range. This method is used for analyzing of the signal values in the spectrum on frequencies on which the Discrete Fourier Transform (DFT) was calculated. Most often the real value of the  $F_0$  is not there on the frequencies where DFT is calculated, but lies between the two spectrum samples. That causes the frequency estimation error that lies in the interval  $[-(F_S/(2N)) \text{ Hz}, (F_S/(2N)) \text{ Hz}]$ , where  $F_S$  is the sampling frequency and  $N$  is the DFT window size. One way of reducing the error is determination of the interpolation function and estimation of the spectrum characteristics in an interval between the two samples.

This procedure gives the reconstruction of the spectrum on the base of DFT. The spectrum parameters are then determined by analytic procedures (differentiation, integration, extreme values,...).

Determination of spectral characteristic values between DFT samples is taken as the local convolution of the neighboring DFT samples and interpolation kernel (piece-wise polynomial interpolation) [16-18]. Two methods are frequently used for interpolation: a) the cubic B-spline interpolation [16] and b) the Parametric Cubic Convolution (PCC) interpolation [17]. From the point of view of the fastness of the maximum position estimation the application of PCC interpolation kernel is more suitable, because it is possible to find the maximum position directly (by means of a formula) using the sampled data without convolution being applied. The detailed analysis of the  $F_0$  estimation by means of PCC interpolation is described in the paper [19]. The results of the application of PCC interpolation for determining of the  $F_0$  in the conditions of application of some window in the processing of the discrete speech signal are presented in [20]. Through some simulation procedures algorithm efficiency analyses have been done where, as a quality measure of an algorithm, the Mean Square Error (MSE) has been used. The best results were shown by the algorithm with the implemented Blackman window. The results of the  $F_0$  estimation of the speech signal modeled by SYMPES (Systematic Procedure to Model Speech Signals via Predefined "Envelope and Signature Sequences") method are shown in [21]. The assessment of the  $F_0$  in MP3 codec is given in [22]. Further, in [23] the estimation of the  $F_0$  in speech signal compressed by G.729 algorithm is described. In addition, the author in [23] established the formulae for analytical calculation of the  $F_0$  without convolution. It is made by multiple speed-up procedure for the estimation of  $F_0$ .

Further in this paper there will be presented some results of the  $F_0$  estimation in audio and speech signals compressed by G.729 algorithm in order to determine the  $F_0$  using PCC interpolation kernels (Keys, Greville and two parametric Greville kernel) and some window functions (Hamming, Hanning, Blackman, Rectangular, Kaiser and Triangular window). The estimation of  $F_0$  was performed on the base of the analytical expression from [19] for Keys kernel and from [23] for Greville and two-parametric Greville kernels. As a measure of the quality of interpolation algorithm MSE (Mean Square Error) will be applied. On the base of minimum values of MSE optimum kernel parameters and the corresponding window function will be determined. Afterward the comparison of the estimation of  $F_0$  between G.729 and G.723.1 [23] codecs will be implemented.

This paper is organized as follows: In Section II there is a description of the PCC algorithm. In Section II.A there are definitions of interpolation kernels. In Section II.B the algorithm for determination of optimal kernel parameters is presented. In Section III numerical MSE results in the estimation of  $F_0$  of the speech signal modeled by the G.729 method are presented. The comparative analysis of the results and the choice of the optimal kernel and window function are shown in Section IV. Section V gives the Conclusion.

## II. ALGORITHM OF FUNDAMENTAL FREQUENCY ESTIMATION

Algorithm for the estimation of  $F_0$ , based on the algorithm from [19], is shown in Fig. 1. This algorithm is realized in the following steps:

*Step 1:* Audio or speech signal  $s(n)$  is coded by G.729 coder.

*Step 2:* Coded signal is decoded by G.729 decoder and generises signal  $x(n)$ .

*Step 3:* Window  $w(n)$  whose length is  $N$  applies to decoded signal  $x(n)$ .

*Step 4:* Spectrum  $X(k)$  is calculated by using DFT:

$$X(k) = DFT(x(n)). \quad (1)$$

The spectrum is calculated in discrete points  $k=0, \dots, N-1$ , where  $N$  is the length of DFT. The real spectrum of signals  $x(n)$  is continuous, whereas DFT defines the values of the spectrum at some discrete points.

*Step 5:* By using peak picking algorithm, the position of the maximum of the real spectrum that is between  $k$ -th and  $(k+1)$ -th samples is determined, where the values  $X(k)$  and  $X(k+1)$  are the highest in the specified domain.

*Step 6:* The position of the maximum of the spectrum is calculated by PCC interpolation. The reconstructed function is:

$$X_r(f) = \sum_{i=k-L/2+1}^{k+L/2} p_i \cdot r(f-i), k \leq f \leq k+1, \quad (2)$$

where  $p_i = X(i)$ ,  $r(f)$  is the kernel of interpolation and  $L$  the number of samples that participate in interpolation.

*Step 7:* By differentiation  $X_r(f)$  and zero adjustment the position of maximum is determined; it presents the estimated  $F_0$ , which is marked as  $f_e$ .

The quality of the algorithm for the estimation of  $F_0$  can be also expressed by MSE:

$$MSE = \overline{(f - f_e)^2}, \quad (3)$$

where  $f$  is true  $F_0$  and  $f_e$  is the estimation of  $F_0$ .

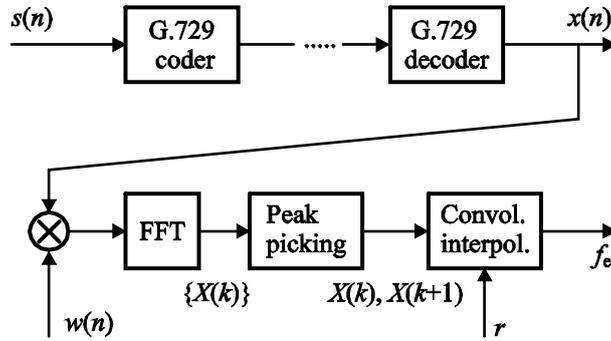


Figure 1. Algorithm for the estimation of  $F_0$ .

#### A. Interpolation Kernel

Next, we give definitions of the interpolation kernels which are tested in this paper:

a) **Keys** interpolation kernel [17,18]:

$$r(f) = \begin{cases} (r+2)|f|^3 - (r+3)|f|^2 + 1, & |f| \leq 1, \\ r|f|^3 - 5r|f|^2 + 8r|f| - 4r, & 1 < |f| \leq 2, \\ 0, & \text{otherwise} \end{cases} \quad (4)$$

For  $L=4$  from Eq. (2) position of maximum is determined:

$$f_{\max} = \begin{cases} k - \frac{c}{2b}, & a = 0 \\ k + \frac{-b + \sqrt{b^2 - ac}}{a}, & a \neq 0 \end{cases}, \quad (5)$$

where:

$$\begin{aligned} a &= 2(rp_{k-1} + (r+2)p_k - (r+2)p_{k+1} - rp_{k+2}) \\ b &= -2rp_{k-1} - (r+3)p_k + (2r+3)p_{k+1} + rp_{k+2} \\ c &= -rp_{k-1} - rp_{k+1} \end{aligned} \quad (6)$$

b) **Greville** interpolation kernel [16]:

$$r(f) = \begin{cases} \left( r + \frac{3}{2} \right) |f|^3 - \left( r + \frac{5}{2} \right) |f|^2 + 1; & \text{if } 0 \leq |f| \leq 1, \\ \frac{1}{2} (r-1) |f|^3 - \left( 3r - \frac{5}{2} \right) |f|^2 + \left( \frac{11}{2} r - 4 \right) |f| - (3r-2); & \text{if } 1 \leq |f| \leq 2, \\ -\frac{1}{2} r |f|^3 + 4r |f|^2 - \frac{21}{2} r |f| + 9r; & \text{if } 2 \leq |f| \leq 3, \\ 0; & \text{if } 3 \leq |f|. \end{cases} \quad (7)$$

For  $L=6$  from Eqs. (2) and (7) position of maximum is determined according to Eq. (5), where:

$$\begin{aligned} a &= -\frac{3}{2} r p_{k-2} + \frac{3}{2} (r-1) p_{k-1} + 3 \left( r + \frac{3}{2} \right) p_k - 3 \left( r + \frac{3}{2} \right) p_{k+1} - \frac{3}{2} (r-1) p_{k+2} + \frac{3}{2} r p_{k+3}; \\ b &= -2r p_{k-2} + (-3r+2) p_{k-1} - (2r+5) p_k + 4(r+1) p_{k+1} - p_{k+2} - r p_{k+3}; \\ c &= -\frac{1}{2} r p_{k-2} + \left( r - \frac{1}{2} \right) p_{k-1} - \left( r - \frac{1}{2} \right) p_{k+1} + \frac{1}{2} r p_{k+2} \end{aligned} \quad (8)$$

c) **Greville** two-parametric cubic convolution kernel (G2P) [16]:

$$r(f) = \begin{cases} \left( r - \frac{5}{2} s + \frac{3}{2} \right) |f|^3 - \left( r - \frac{5}{2} s + \frac{5}{2} \right) |f|^2 + 1; & 0 \leq |f| \leq 1, \\ \frac{1}{2} (r-s-1) |f|^3 - \left( 3r - \frac{9}{2} s - \frac{5}{2} \right) |f|^2 + \left( \frac{11}{2} r - 10s - 4 \right) |f| - (3r-6s-2); & 1 \leq |f| \leq 2, \\ -\frac{1}{2} (r-3s) |f|^3 + \left( 4r - \frac{25}{2} s \right) |f|^2 - \left( \frac{21}{2} r - 34s \right) |f| + (9r-30s); & 2 \leq |f| \leq 3, \\ -\frac{1}{2} s |f|^3 + \frac{11}{2} s |f|^2 - 20s |f| + 24s; & 4 \leq |f|. \end{cases} \quad (9)$$

For  $L=8$  from Eqs. (2) and (9) position of maximum is determined according to Eq. (5), where:

$$\begin{aligned} a &= -\frac{3}{2} s p_{k-3} - \frac{3}{2} (r-3s) p_{k-2} + \frac{3}{2} (r-s-1) p_{k-1} + 3 \left( r - \frac{5}{2} s + \frac{3}{2} \right) p_k - 3 \left( r - \frac{5}{2} s + \frac{3}{2} \right) p_{k+1} \\ &\quad - \frac{3}{2} (r-s-1) p_{k+2} + -\frac{3}{2} (r-3s) p_{k+3} + \frac{3}{2} s p_{k+4}; \\ b &= -2s p_{k-3} - (2r-7s) p_{k-2} + (-3r+6s+2) p_{k-1} - \left( 2r-5s + \frac{5}{2} \right) p_k + (4r-10s+1) p_{k+1} \\ &\quad + (3s-1) p_{k+2} + (-r+2s) p_{k+3} - s p_{k+4}; \\ c &= -\frac{1}{2} s p_{k-3} + \left( -\frac{1}{2} r + 2s \right) p_{k-2} + \left( r - \frac{5}{2} s - \frac{1}{2} \right) p_{k-1} - \\ &\quad \left( r + \frac{5}{2} s + \frac{1}{2} \right) p_{k+1} + \left( \frac{1}{2} r - 2s \right) p_{k+2} + \frac{1}{2} s p_{k-3} \end{aligned} \quad (10)$$

In the Eqs. (4)-(10) there are  $\alpha$  and  $s$  parameters. The optimal values of these parameters will be determined by the minimal value of MSE, for Keys, Greville and G2P kernel. For the first two of them:

$$r_{opt} = \arg \min_r (MSE), \quad (11)$$

and for the G2P kernel:

$$(\gamma_{opt}, S_{opt}) = \arg \min_{\gamma, S} (MSE). \quad (12)$$

The detailed analysis in [19-23] showed that the minimal value of MSE depends on the application of window by which signal processing  $x(n)$  is carried out in time domain. MSE will be defined for: a) Hamming, b) Hanning, c) Blackman, d) Rectangular, e) Kaiser and f) Triangular window.

### B. Interpolation Kernel Parameters

Algorithm for determination of interpolation kernel parameters  $\gamma$  and  $S$  is realized in the following steps:

*Step 1:* signal  $x(n)$ , which was previously coded and decoded by G.729 algorithm, is modified by the window function  $w(n)$  whose length is  $N$ ,

*Step 2:* spectrum  $X(k)$  is determined by the application of DFT,

*Step 3:* reconstruction of the continual function that represents spectrum  $X(f)$  is performed by the application of PCC interpolation,

*Step 4:* MSE is calculated for various values of parameters  $\gamma$  and  $S$  depending on the implemented window,

*Step 5:*  $\gamma_{opt}$  and  $S_{opt}$  are determined for which minimal value of MSE is obtained.

### C. Test Signals

PCC algorithm of the estimation of  $F_0$  will be applied to: i) simulation Sine test signal, and ii) Speech test signal. Simulation Sine signal for testing of PCC algorithm is defined in [19]:

$$s(t) = \sum_{i=1}^K \sum_{g=0}^M a_i \sin \left( 2\pi f_i \left( f_o + g \frac{f_s}{NM} \right) t + \phi_i \right). \quad (13)$$

where  $f_0$  is fundamental frequency,  $\phi_i$  and  $a_i$  are phase and amplitude of the  $i$ -th harmonic, respectively,  $K$  is the number of harmonics,  $M$  is the number of points between the two samples in spectrum where PCC interpolation is being made. The Speech test signal is obtained by recording of a speaker in the real acoustic ambient. For further comparative analysis by interpolation it is suitable for the  $F_0$  of the Speech test signal and the one of the Sine test signal to be equal. PCC algorithm will be applied to:

- a) uncoded simulation Sine and Speech test signals, and
- b) by G.729 algorithm coded and decoded Sine and Speech test signals.

## III. EXPERIMENTAL RESULTS AND COMPARISON

### A. Testing Parameters

In the simulation process  $f_0$  and  $\phi_i$  are random variables with uniform distribution in the range [G2 (97.99 Hz), G5 (783.99 Hz)] and  $[0, 2\pi]$ . Signal frequency of sampling is  $f_s=8$  kHz and the length of window is  $N=256$ , which assures the analysis of subsequences that last 32 ms. The results presented further in this paper relate to  $f_0=125$ -140.625Hz (frequencies between the eighth and ninth DFT components). Number of frequencies in the specified range for which the estimation is done is  $M=100$ . The Sine test signal is with  $K=10$  harmonics. All further analyses will relate to a) Hamming, b) Hanning, c) Blackman, d) Rectangular, e) Kaiser and f) Triangular window.

### B. Experimental Results

#### 1) Keys Kernel

Applying an algorithm for determination of parameters of Keys interpolation kernel some diagrams are drawn  $MSE(\gamma)$ , the minimum value  $MSE_{Kmin}$  determined, and on the base of it the optimum value of Keys kernel  $\gamma_{opt}$  determined for: a) Hamming (Fig. 2), b) Hann, c) Blackman, d) Rectangular, e) Kaiser, and f) Triangular window functions. Values  $MSE_{Kmin}$  and  $\alpha_{opt}$  are presented in Table I (uncoded Sine test signal  $MSE_{Kmin}$ , G.729 coded Sine test signal  $MSE_{KGmin}$ ) and Table II (Speech test signal  $MSE_{KSPmin}$ , G.729 coded Sine test signal  $MSE_{KSGPmin}$ ). For the comparison, the results of the G.723.1 in Tables I - II are given as well. These results are obtained under identical circumstances as in [23].

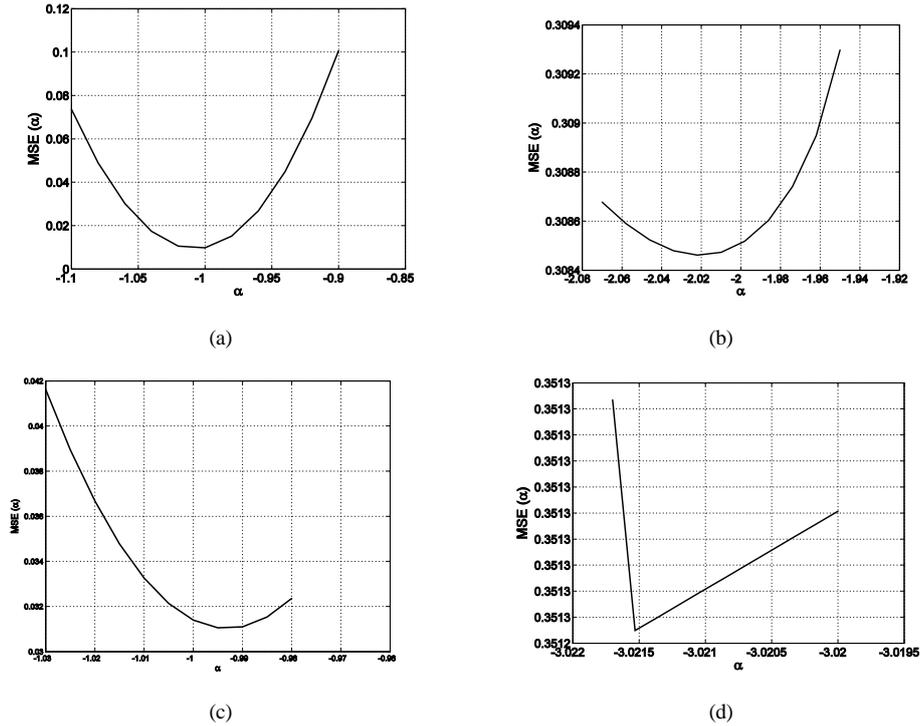


Figure 2. MSE( $r$ ) for Keys kernel and Hamming window: a) uncompressed Sine test signal, b) G.729 compressed Sine test signal, c) uncompressed Speech test signal, d) G.729 compressed Speech test signal.

TABLE I. MINIMUM MSE AND  $\alpha_{opt}$  FOR SINE TEST SIGNAL (KEYS KERNEL).

| Window      | Uncoded signal |                     | Signal coded by G.723.1 algorithm |                      | Signal coded by G.729 algorithm |                      |
|-------------|----------------|---------------------|-----------------------------------|----------------------|---------------------------------|----------------------|
|             | $\Gamma_{opt}$ | MSE <sub>Kmin</sub> | $\Gamma_{opt}$                    | MSE <sub>KGmin</sub> | $\Gamma_{opt}$                  | MSE <sub>KGmin</sub> |
| Hamming     | -1             | 0.0098              | -0.875                            | 0.4203               | -2.0220                         | 0.3085               |
| Hanning     | -0.880         | 0.000619            | -0.820                            | 0.4170               | -2.0400                         | 0.3341               |
| Blackman    | -0.800         | 0.000423            | -0.760                            | 0.4137               | -1.8286                         | 0.3422               |
| Rectangular | -2.680         | 0.1767              | -1.740                            | 0.3855               | -3.2000                         | 0.2481               |
| Kaiser      | -1.140         | 0.0066              | -1                                | 0.3887               | -2.1000                         | 0.2963               |
| Triangular  | -1.010         | 0.0036              | -0.970                            | 0.3982               | -2.0000                         | 0.3063               |

TABLE II. MINIMUM MSE AND  $\alpha_{opt}$  FOR SPEECH TEST SIGNAL (KEYS KERNEL).

| Window      | Uncoded signal |                       | Signal coded by G.723.1 algorithm |                        | Signal coded by G.729 algorithm |                        |
|-------------|----------------|-----------------------|-----------------------------------|------------------------|---------------------------------|------------------------|
|             | $\Gamma_{opt}$ | MSE <sub>KSPmin</sub> | $\Gamma_{opt}$                    | MSE <sub>KGSPmin</sub> | $\Gamma_{opt}$                  | MSE <sub>KGSPmin</sub> |
| Hamming     | -0.995         | 0.0310                | -1.020                            | 0.9351                 | -3.0215                         | 0.3513                 |
| Hanning     | -0.880         | 0.0349                | -0.920                            | 1.0523                 | -2.9950                         | 0.3664                 |
| Blackman    | -0.800         | 0.0358                | -0.840                            | 1.0213                 | -2.8200                         | 0.3752                 |
| Rectangular | -2.400         | 0.4323                | -2.100                            | 0.6752                 | -4.0100                         | 0.3243                 |
| Kaiser      | -1.080         | 0.0339                | -1.150                            | 0.9390                 | -3                              | 0.3426                 |
| Triangular  | -1.030         | 0.0277                | -1.040                            | 0.9865                 | -2.8420                         | 0.3385                 |

On the base of the results presented in Tables I - II it is obvious that:

a) at Sine test signal the greatest precision of  $F_0$  estimation is when Blackman window (MSE<sub>Kmin</sub>=0.000423) is applied. At G.723.1 coded Sine test signal the greatest precision of estimation is in Rectangular (MSE<sub>KGmin</sub>=0.3855) window. When G.723.1 coding is applied, the precision in  $F_0$  estimation is lowered for MSE<sub>KGmin</sub>/MSE<sub>Kmin</sub>=0.3855/0.000423=91.134 times.

At G.729 coded Sine test signal the greatest precision of estimation is in Rectangular (MSE<sub>KGmin</sub>=0.2481) window. When G.729 coding is applied, the precision in  $F_0$  estimation is lowered for MSE<sub>KGmin</sub>/MSE<sub>Kmin</sub>=0.2481/0.000423=58.652 times.

b) at Speech test signal the greatest precision is in Triangular window ( $MSE_{KSPmin}=0.0277$ ). At G.723.1 coded Speech signal the greatest precision is in Rectangular window ( $MSE_{KGSPPmin}=0.6752$ ). When coding is applied, the precision in  $F_0$  estimation is lowered for  $MSE_{KGSPPmin}/MSE_{KSPmin}=0.6752/0.0277=24.375$  times.

At G.729 coded Speech test signal the greatest precision of estimation is in Rectangular ( $MSE_{KGmin}=0.3243$ ) window. When G.729 coding is applied, the precision in  $F_0$  estimation is lowered for  $MSE_{KGmin}/MSE_{Kmin}=0.3243/0.0277= 11.707$  times.

c) at G.723.1 coded Speech signal in relation to coded Sine signal inaccuracy in  $F_0$  estimation is greater for  $MSE_{KGSPPmin}/MSE_{KGmin}=0.6752/0.3855=1.751$  times.

At G.729 coded Speech signal in relation to coded Sine signal inaccuracy in  $F_0$  estimation is greater for  $MSE_{KGSPPmin}/MSE_{KGmin}=0.3243/0.2481=1.307$  times.

## 2) Greville Kernel

Applying algorithm for determination of Greville interpolation kernel some diagrams  $MSE(\alpha)$  are drawn, minimum value  $MSE_{Gmin}$  determined, and on the base of it optimum value of Greville kernel parameters  $\alpha_{opt}$  determined for: a) Hamming (Fig. 3), b) Hann, c) Blackman, d) Rectangular, e) Kaiser, and f) Triangular window. Values  $MSE_{min}$  and  $\alpha_{opt}$  are presented in Table III (uncoded Sine test signal  $MSE_{Gmin}$ , coded Sine test signal  $MSE_{GGmin}$ ) and Table IV (Speech test signal  $MSE_{GSPmin}$ , coded Speech test signal  $MSE_{GGSPmin}$ ). For the comparison, the results of the G.723.1 in Tables III - IV are given as well. These results are obtained under identical circumstances as in [23].

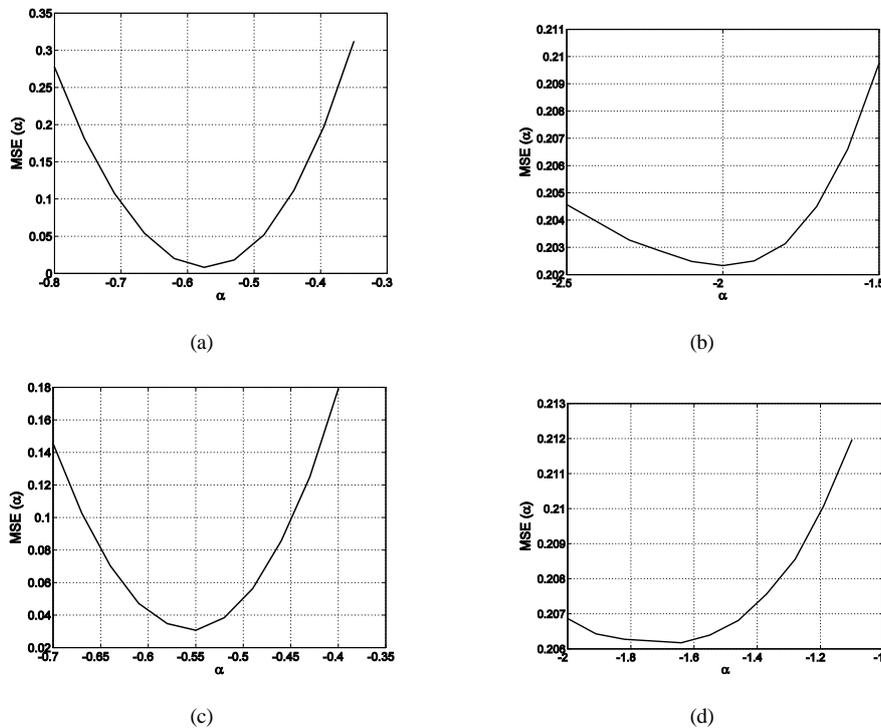


Figure 3.  $MSE(\alpha)$  for Greville kernel and Hamming window: a) uncompressed Sine test signal, b) G.729 compressed Sine test signal, c) uncompressed Speech test signal, d) G.729 compressed Speech test signal.

TABLE III. MINIMUM MSE AND  $\alpha_{opt}$  FOR SINE TEST SIGNAL (GREVILLE KERNEL).

| Window      | Uncoded signal |              | Signal coded by G.723.1 algorithm |               | Signal coded by G.729 algorithm |               |
|-------------|----------------|--------------|-----------------------------------|---------------|---------------------------------|---------------|
|             | $\alpha_{opt}$ | $MSE_{Gmin}$ | $\alpha_{opt}$                    | $MSE_{GGmin}$ | $\alpha_{opt}$                  | $MSE_{GGmin}$ |
| Hamming     | -0.560         | 0.0089       | -0.4800                           | 0.3841        | -2                              | 0.2023        |
| Hanning     | -0.450         | 0.0006573    | -0.3900                           | 0.3969        | -2.1750                         | 0.2118        |
| Blackman    | -0.410         | 0.0002441    | -0.3650                           | 0.3938        | -1.8100                         | 0.2149        |
| Rectangular | -2.300         | 0.1472       | -1.3000                           | 0.3274        | -3.1300                         | 0.2062        |
| Kaiser      | -0.660         | 0.0059       | -0.5400                           | 0.3598        | -2.1000                         | 0.1964        |
| Triangular  | -0.575         | 0.0007793    | -0.5000                           | 0.3659        | -2.0250                         | 0.1962        |

TABLE IV. MINIMUM MSE AND  $\alpha_{opt}$  FOR SPEECH TEST SIGNAL (GREVILLE KERNEL).

| Window      | Uncoded signal |                 | Signal coded by G.723.1 algorithm |                 | Signal coded by G.729 algorithm |                 |
|-------------|----------------|-----------------|-----------------------------------|-----------------|---------------------------------|-----------------|
|             | $\Gamma_{opt}$ | $MSE_{GGSPmin}$ | $\Gamma_{opt}$                    | $MSE_{GGSPmin}$ | $\Gamma_{opt}$                  | $MSE_{GGSPmin}$ |
| Hamming     | -0.560         | 0.0310          | -0.6400                           | 0.7983          | -1.6400                         | 0.2062          |
| Hanning     | -0.450         | 0.0363          | -0.5300                           | 0.9201          | -1.6200                         | 0.2042          |
| Blackman    | -0.410         | 0.0344          | -0.5100                           | 0.9209          | -1.6750                         | 0.2041          |
| Rectangular | -2.100         | 0.2016          | -1.7000                           | 0.5178          | -2.1000                         | 0.2268          |
| Kaiser      | -0.660         | 0.0255          | -0.7800                           | 0.7787          | -1.9600                         | 0.2080          |
| Triangular  | -0.575         | 0.0256          | -0.6750                           | 0.8011          | -1.7600                         | 0.2071          |

On the base of the results presented in Tables III - IV it is obvious that:

a) at Sine test signal the greatest precision of  $F_0$  estimation is when Blackman ( $MSE_{Gmin}=0.0002441$ ) window is applied. At G.723.1 coded Sine test signal the greatest precision of estimation is in Rectangular window ( $MSE_{GGmin}=0.3274$ ). When coding is applied, the precision of  $F_0$  estimation is lowered for  $MSE_{GGmin}/MSE_{Gmin}=0.3274/0.0002441=1341.25$  times.

At G.729 coded Sine test signal the greatest precision of estimation is in Triangular window ( $MSE_{GGmin}=0.1962$ ). When coding is applied, the precision of  $F_0$  estimation is lowered for  $MSE_{GGmin}/MSE_{Gmin}=0.1962/0.0002441=803.768$  times.

b) at Speech test signal the greatest precision is in Kaiser window ( $MSE_{GSPmin}=0.0255$ ). At G.723.1 coded Speech signal the greatest precision is in Rectangular window ( $MSE_{GGSPmin}=0.5178$ ). When G.723.1 coding is applied, the precision of  $F_0$  estimation is lowered for  $MSE_{GGSPmin}/MSE_{GSPmin}=0.5178/0.0255=20.3$  times.

At G.729 coded Speech signal the greatest precision is in Blackman window ( $MSE_{GGSPmin}=0.2041$ ). When G.729 coding is applied, the precision of  $F_0$  estimation is lowered for  $MSE_{GGSPmin}/MSE_{GSPmin}=0.2041/0.0255=8.003$  times.

c) at G.723.1 coded Speech signal in relation to coded Sine signal inaccuracy of the  $F_0$  is greater for  $MSE_{GGSPmin}/MSE_{GGmin}=0.5178/0.3274=1.58$  times.

At G.729 coded Speech signal in relation to coded Sine signal inaccuracy of the  $F_0$  is greater for  $MSE_{GGSPmin}/MSE_{Gmin}=0.2041/0.1962=1.04$  times.

### 3) G2P Kernel

For window (Blackman, Triangular, Kaiser and Blackman) which showed the best results at G.729 coding with Greville kernel, an analysis was performed by means of G2P kernel. Three-dimensional  $MSE(r,s)$  graphics are drawn (Figs. 4.a, 5.a, 6.a, and 7.a), the shift of minimum  $MSE_{min}$  in  $(r,s)$  level determined, and  $r_{opt}$  and  $s_{opt}$  values determined and presented in Table V. Furthermore, it gives the results for the G.723.1 codec from [23]. In Figs 4.b, 5.b, 6.b, and 7.b the positions of  $MSE_{min}=MSE(r_{opt},s_{opt})$  minimum in  $(r,s)$  plane for Greville (point A) and G2P (point B) interpolation kernel, are shown. Vector  $\overline{AB}$  shows the position change of minimum ( $MSE(\alpha_{opt},s_{opt})$ ).

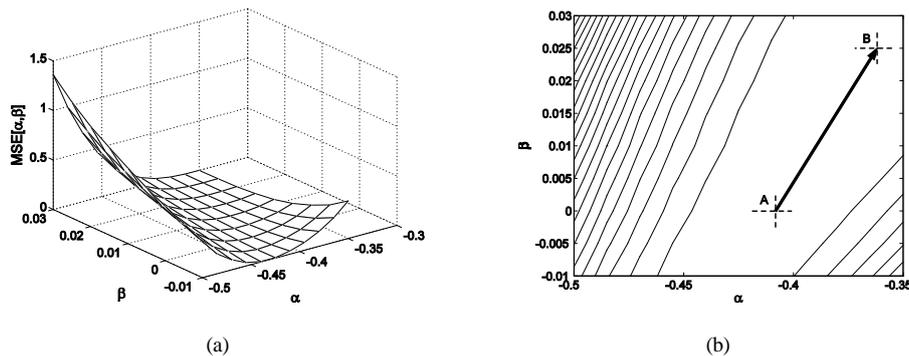


Figure 4. Sine test signal without compression with the application of Blackman window: a)  $MSE(\alpha, \beta)$  for G2P PCC interpolation, b) positions of min ( $MSE(\alpha_{opt}, \beta_{opt})$ ) in plane  $(\alpha, \beta)$  for Greville (point A) and G2P PCC (point B) interpolation.

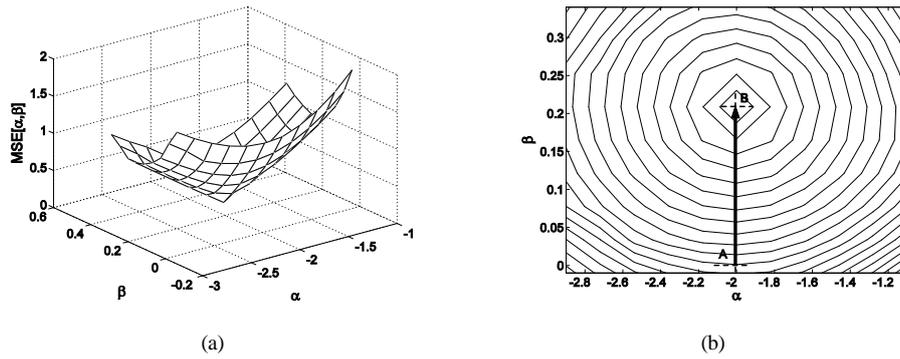


Figure 5. Sine test signal with G.729 compression with the application of Triangular window: a)  $MSE(\alpha, \beta)$  for the application of G2P PCC interpolation, b) Positions of min ( $MSE(\alpha, \beta)$ ) in plane ( $\alpha, \beta$ ) for Greville (point A) and G2P PCC (point B) interpolation.

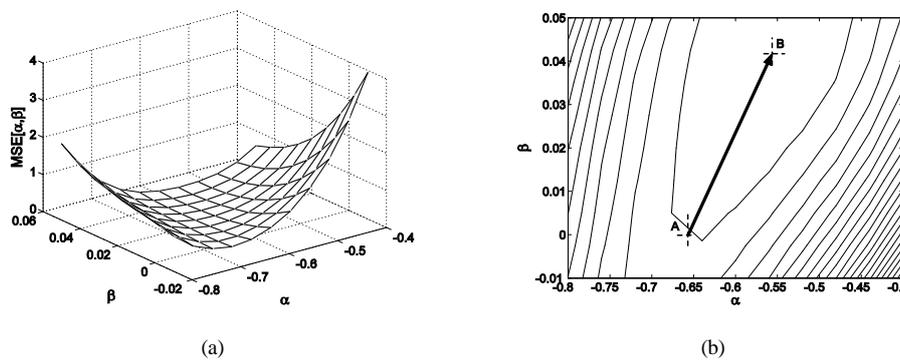


Figure 6. Speech test signal without compression with the application of Kaiser window: a)  $MSE(\alpha, \beta)$  for G2P PCC interpolation, b) positions of min ( $MSE(\alpha, \beta)$ ) in plane ( $\alpha, \beta$ ) for Greville (point A) and G2P PCC (point B) interpolation.

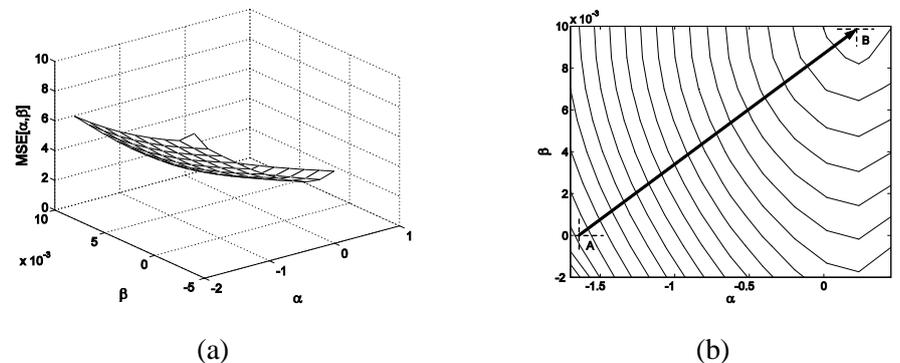


Figure 7. Speech test signal with G.729 compression with the application of Blackman window: a)  $MSE(\alpha, \beta)$  for the application of G2P PCC interpolation, b) Positions of min ( $MSE(\alpha, \beta)$ ) in plane ( $\alpha, \beta$ ) for Greville (point A) and G2P PCC (point B) interpolation.

TABLE V. MINIMUM MSE,  $\Gamma_{opt}$  AND  $S_{opt}$  (G2P KERNEL).

|                    |                              | $\Gamma_{opt}$ | $S_{opt}$ | $MSE_{G2Pmin}$          |
|--------------------|------------------------------|----------------|-----------|-------------------------|
| Sine test signal   | Uncoded signal Blackman win. | -0.3650        | 0.0250    | $MSE_{G2Pmin}=0.00014$  |
|                    | G.723.1 coded Rectang. win.  | -0.95          | 0.1838    | $MSE_{G2PGmin}=0.1750$  |
|                    | G.729 coded Triang. win.     | -2             | 0.2088    | $MSE_{G2PGmin}=0.1676$  |
| Speech test signal | Uncoded signal Kaiser win.   | -0.5600        | 0.0425    | $MSE_{G2PSmin}=0.0198$  |
|                    | G.723.1 coded Rectang. win.  | -1.08          | 0.260     | $MSE_{G2PGSmin}=0.2898$ |
|                    | G.729 coded Blackman. win.   | 0.2350         | 0.01      | $MSE_{G2PGSmin}=0.1145$ |

On the base of the results presented in Table. V it is obvious that:

a) at Sine test signal the greatest precision of  $F_0$  estimation (Greville interpolation kernel) is when Blackman ( $MSE_{Gmin}=0.0002441$ ) window is applied. When G2P interpolation ( $MSE_{G2Pmin}=0.00014$ ) is applied, the precision of  $F_0$  estimation is increased for  $MSE_{Gmin}/MSE_{G2Pmin}=0.0002441/0.00014=1.74$  times.

b) at G.723.1 coded Sine test signal the greatest precision of estimation (Greville interpolation kernel) is in Rectangular window ( $MSE_{GG}=0.3274$ ). When G2P interpolation ( $MSE_{G2Pmin}=0.175$ ) is applied, the precision of  $F_0$  estimation is increased for  $MSE_{GGmin}/MSE_{G2Pmin}=0.3274/0.175=1.87$  times.

c) at G.729 coded Sine test signal the greatest precision of estimation (Greville interpolation kernel) is in Triangular window ( $MSE_{GG}=0.1962$ ). When G2P interpolation ( $MSE_{G2Pmin}=0.1676$ ) is applied, the precision of  $F_0$  estimation is increased for  $MSE_{GGmin}/MSE_{G2Pmin}=0.1962/0.1676=1.17$  times.

d) at Speech test signal the greatest precision of the  $F_0$  estimation (Greville interpolation kernel) is when Kaiser ( $MSE_{GSPmin}=0.0255$ ) window is applied. When G2P interpolation ( $MSE_{G2PSPmin}=0.0198$ ) is applied, the precision of  $F_0$  estimation is increased for  $MSE_{GSPmin}/MSE_{G2PSPmin}=0.0255/0.0198=1.28$  times.

e) at G.723.1 coded Speech test signal the greatest precision of estimation (Greville interpolation kernel) is in Rectangular window ( $MSE_{GGSPmin}=0.5178$ ). When G2P interpolation ( $MSE_{G2PSPmin}=0.2898$ ) is applied, the precision of  $F_0$  estimation is increased for  $MSE_{GGSPmin}/MSE_{G2PSPmin}=0.5178/0.2898=1.78$  times.

f) at G.729 coded Speech test signal the greatest precision of estimation (Greville interpolation kernel) is in Blackman window ( $MSE_{GGSPmin}=0.2041$ ). When G2P interpolation ( $MSE_{G2PGSPmin}=0.1145$ ) is applied, the precision of  $F_0$  estimation is increased for  $MSE_{GGSPmin}/MSE_{G2PGSPmin}=0.2041/0.1145=1.78$  times.

g) at G.723.1 coded Speech signal in relation to G.723.1 coded Sine signal, the inaccuracy of  $F_0$  estimation is greater for  $MSE_{G2PGSPmin}/MSE_{G2Pmin}=0.2898/0.175=1.656$  times.

h) at G.729 coded Speech signal in relation to G.729 coded Sine signal, the inaccuracy of  $F_0$  estimation is greater for  $MSE_{G2PGSPmin}/MSE_{G2Pmin}=0.1676/0.1145=1.463$  times.

#### IV. COMPARATIVE ANALYSIS

Comparative precision analysis of the estimated  $F_0$  of the Sine test signal and the Speech test signal, without and with G.729 compression will be performed on the base of the minimal values of MSE. The minimal value of MSE is determined on the base of a diagram in the Fig. 2 (Keys), Fig. 3 (Greville) and Figs. 4 - 7 (G2P) and presented in the Table I ( $MSE_{Kmin}$ ,  $MSE_{KGmin}$ ), Table II ( $MSE_{KSPmin}$ ,  $MSE_{KGGSPmin}$ ), Table III ( $MSE_{Gmin}$ ,  $MSE_{GGmin}$ ), Table IV ( $MSE_{GSPmin}$ ,  $MSE_{GGSPmin}$ ) and Table V ( $MSE_{G2Pmin}$ ,  $MSE_{G2PGmin}$ ,  $MSE_{G2PSPmin}$ ,  $MSE_{G2PGSPmin}$ ) respectively. Furthermore the comparative analysis of the  $F_0$  estimation with G.729 and G.723.1 algorithms will be made.

Comparing the values  $MSE_{min}$  from Tables. I - V it can be concluded that:

a) the optimum choice for Sine test signal (without compression) is Blackman window for all interpolation kernels. G2P interpolation kernel, which generates 66.91% less than Keys and 42.65% less than Greville kernel, showed the best results.

b) the optimum choice for Speech test signal is G2P kernel with Kaiser window, which generates 59.57% less than Keys kernel (Triangular window) and 56.08% less than Greville kernel (Kaiser window).

c) the optimum choice for Sine test signal coded by G.723.1 algorithm is Rectangular window for all interpolation kernels. G2P interpolation kernel, which generates 54.61% less than Keys and 46.55% less than Greville kernel, showed the best results.

d) the optimum choice for Speech test signal coded by G.723.1 algorithm is rectangular window for all interpolation kernels. G2P interpolation kernel, which generates 57.21% less than Keys and 44.04% less than Greville kernel, showed the best results.

e) the optimum choice for Sine test signal coded by G.729 algorithm is G2P interpolation kernel with Triangular window, which generates 32.41% less than Keys (Rectangular window) and 14.57% less than Greville kernel (Triangular window), showed the best results

f) the optimum choice for Speech test signal coded by G.729 algorithm is G2P interpolation kernel with Blackman window, which generates 64.66% less than Keys (Rectangular window) and 43.9% less than Greville kernel (Blackman window), showed the best results.

g) comparing MSE for G2P kernel for uncoded Speech test signal (Kaiser window,  $MSE_{G2PSPmin}=0.0198$ ), G.723.1 coded Speech signal (Rectangular window,  $MSE_{G2PGSPmin}=0.2898$ ) and G.729 coded Speech signal (Blackman window,  $MSE_{G2PGSPmin}=0.1145$ ), in relation to  $MSE_{G2PGSPmin}/MSE_{G2PSPmin}=0.2898/0.0198=14.636$  and  $MSE_{G2PGSPmin}/MSE_{G2PSPmin}=0.1145/0.0198=5.78$  has been obtained.

It is clear that the accuracy of the G.729 algorithm is considerably higher compared to the G.723.1 algorithm. Precisely, it is higher for  $14.636/5.78 = 2.532$  times.

In accordance to the derived conclusion, the application of the algorithm for further processing of G.723.1 coded signal with algorithms based on the estimated  $F_0$  (automatic verification of a speaker, recognition of the Speech etc.) would not bring satisfactory results [23], while processing of G.729 coded signal causes significantly smaller error. The obtained results recommend using PCC algorithm with G2P kernel in preprocessing signals compressed by G.729 method for further processing by algorithms which require a precise determination of the  $F_0$ .

## V. CONCLUSION

This paper presented the analysis of the  $F_0$  estimation results of the Speech signal compressed by G.729 algorithm which has been intensively used in VoIP services. The estimation of the  $F_0$  has been made by Peaking Peaks algorithm with implemented PCC interpolation. Experiments have been performed with Keys, Greville and Greville two-parametric G2P kernels. In order to minimize MSE some windows have been implemented. The detailed analysis has shown that the optimal choice is Greville two-parametric kernel and the Blackman window implemented in PCC algorithm. In relation to Keys and Greville kernels, Greville two-parametric kernel generates 64.66% and 43.9% less MSE, respectively. Comparing the obtained results to the results of the estimation of the  $F_0$  in the Speech signal that is not modeled by G.729 method, a relation of minimal MSEs 5.78 has been obtained. The obtained results recommend using of PCC algorithm with G2P kernel in preprocessing of signals compressed by G.729 method for further processing by algorithms which require a precise determination of the  $F_0$  (automatic verification of the speaker, recognition of the speech, etc.).

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